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INELASTIC SCATTERING IN URANIUM

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ABSTRACT

The distribution curves in paraffin for neutrons from Ra-Be and Ra-B sources as modified by passing through 4.7 cm of uranium have been analyzed. The results indicate an upper limit to the inelastic scattering cross section of Ra-Be neutrons in uranium of 2.5 barns and a degradation of energy to an average of about 200 Kev. The corresponding qualities for Ra-B neutrons are 2.4 barns and 100 Kev.

INELASTIC SCATTERING IN URANIUM

Two separate measurements have been made of the distribution of indium resonance neutrons in paraffin with a central cavity of 12 cm radius containing the source[1]. These measurements were made with and without a 4.7 cm thick uranium sphere surrounding the source in order to determine the fast fission effect. However, the shape of the curves[2] suggests that two fairly distinct groups of neutrons are present: those which have lost no energy in passing through the uranium and those which have been inelastically scattered. From these data it is possible to secure information concerning the amount of inelastic scattering and the energy loss involved.

The nature of the slowing-down process in hydrogenous materials is such that if a source emits two groups of neutrons of appreciably different average energy, the density of resonance or thermal neutrons at a large distance from the source is determined almost completely by the higher-energy group. It therefore follows that if the introduction of material around a source produces a new source with these characteristics, it is possible to analyze the distribution curves corresponding to the two groups.

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1) E. R. Graves and J. H. Manley, CP-257.
   B. Feld et al, CF-1177.

2) See curves A_u of Fig. 1.
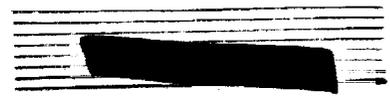
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In a material in which there is neither capture nor production of neutrons the effect of surrounding a source with such a material is simply that a fraction f of the source neutrons escapes without energy loss, while the fraction, $I = 1 - f$ is inelastically scattered. If the energy loss in inelastic scattering is sufficient so that the range of these neutrons in the slowing medium is considerably less than that of the primary neutrons, then the ordinates of the distribution curve with material present are simply reduced by the factor f at large distances. Specifically, if

$A_o(r)$ = activity due to source alone

$A_u(r)$ = activity with material around source

$A_i(r)$ = activity attributed to inelastically scattered neutrons

then

$$\int A_o r^2 dr = \int A_u r^2 dr = \int A_i r^2 dr + f \int A_o r^2 dr$$

or, dividing by the left hand term

$$1 = I + f \qquad \text{where} \quad I = \int A_i r^2 dr \Big/ \int A_o r^2 dr$$

In the case of capture, f as determined from the activity at large distances is unaltered and this is also true in the case of production providing the new neutrons have an energy less than that of the primaries so that they do not contribute to A_u at large distances. However, it is no longer true in either case that

$$\int A_o r^2 dr = \int A_u r^2 dr$$
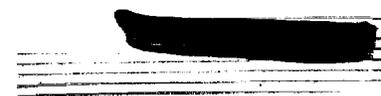
but I is still the fraction which has made collisions leading to inelastic
scattering, capture, fission or combinations of these.

In the present case of normal uranium and a fast neutron source,
capture is negligible and the production small. The production may be measured
by

$$E \;=\; \int A_u r^2 dr \Big/ \int A_o r^2 dr$$

and the activity due to fission neutrons denoted as A_f in order to separate
it in discussion from A_i. Consideration of the shape of the difference distri-
bution $A_i + A_f = A_u - f A_o$ is perturbed by fission neutrons (and capture in
producing fission) but not to the full extent of A_f since the fission neutrons
are also inelastically scattered. In the cases to be considered this results
in a negligible perturbation since E is not much greater than one. Consequently
valid conclusions from the difference distribution can be drawn essentially by
neglecting the small term, A_f.

The procedure is to determine f from A_u/A_o at large r from which
I and the inelastic scattering cross section follow. The difference distribu-
tion $A_u - f A_o$ is then examined to obtain estimates of the energy of the
inelastically scattered neutrons. This analysis is applied to the data of
CF-1177.

There are two methods which may be applied to the difference distri-
bution in order to obtain an estimate of the energy of the inelastically scattered
neutrons:

(1) Beyond a transition distance, $\log A r^2$ is linear with r and the
slope, α, is a function of the neutron energy. This function has been

determined with sources of neutrons of different energy and is given in CF-209.
The calibration applies to a point source in water whereas the present data
pertain to the distribution about a cavity in paraffin. However, these data
include the distribution for a Ra-Be source and the α therefrom is identical
with that obtained from a similar source completely surrounded with water. In
this case the cavity has compensated the greater hydrogen density of paraffin and
consequently the curve of CF-209 has been used directly.

(2) The $\overline{r^2}$ of a distribution in hydrogenous material is also a measure
of the energy. The relation is given in CP-1251, again for a point source in
water. Serber (LAA M-8) has computed the effect of a cavity in the form:

$$x' = x + 1/2 - 1/3\left[e^x - \frac{2}{\sqrt{\pi}} x^{1/2} F(1,3/2,x)\right]$$

where

$$x' = \overline{r^2}/6a^2 \qquad \overline{r^2} \text{ as measured with cavity}$$

$$a = \text{radius of cavity}$$

and

$$x = \overline{r_o^2}/6a^2 \qquad \overline{r_o^2} \text{ as measured without cavity}$$

This expression is then used to determine $\overline{r_o^2}$ in paraffin and this value
corrected to water in order to use the curves relating $\overline{r_o^2}$ to energy given
in CP-1251.

Ra-Be Data

For $r > 20$ cm each measured point for A_u can be fitted within less
than 3% by

$$A_u r^2 = Be^{-0.288r} + 0.60Ae^{-0.105r}$$

The last term is an accurate representation of $0.60\ A_o r^2$ in this range; that is,

$$A_u r^2 = A_i r^2 + f A_o r^2$$

The $A_i r^2$ curve shown in Fig. 1 illustrates the very good exponential character at large r. Therefore, $f = 0.60$ and $I = 0.40$. From this value of f an upper limit of the cross section σ can be determined using the thickness of the sphere R:

$$I = 1 - e^{-n\sigma R}$$

from which $\sigma = 3.0$ b. This cross section is for all processes except elastic scattering, in this case, inelastic scattering, σ_i, plus fission σ_f. For both Ra-Be and Ra-B $\sigma_f = 0.5$, hence $\sigma_i = 2.5$. This value is in reasonably good agreement with 2.7 obtained with Ra-Be neutrons and a fission detector. The result 2.3 has been obtained for the total inelastic scattering for 3 Mev neutrons. The agreement must be fortuitous since the effect of multiple scattering is not negligible and therefore 3.0 b must be considered as an upper limit.

The energy as determined by the slope method is obtained using $\alpha = 0.288$. The $\overline{r^2}$ values have been calculated by integration of the corresponding distribution curves. The results are given in Table I.

Ra-B Data

These data have been treated in an identical fashion, but there is not such a sharp distinction between primary and degraded neutrons. This may be due to the shorter range of available data, but it is definitely suggested in

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the shape of the original curves as well as in the difference curve of Fig. 1.
As a result, the value of f and the average energy of the inelastically scat-
tered neutrons are less certain. The tabulation is given in Table II. The
value of α in this table is that indicated by the dotted line of curve B,
Fig. 1.

Discussion

The agreement between the α and $\overline{r_0^2}$ methods of energy determina-
tion is better than could be anticipated. The nature of the methods is such
that the α procedure will give a higher energy than the true average. The
energy from $\overline{r_0^2}$ also weights the high energy part of a distribution. The
results by this method may be suspected of being high for an additional reason,
that $\overline{r_0^2}$ for Ra-Be in Table I is 5-10% higher than the usual value obtained
for a point source in water. Better agreement would not be expected from the
approximations involved in the correction for the cavity. At first thought the
change of $\overline{r^2}$ from 295 to 584 (Table I) due to a cavity with an a^2 of 139
might be considered unreasonable. However, if one considers the cavity effect
as an extension of the first mean free path the fact that subsequent paths are
distributed at random with respect to this initial direction suggests that a
cavity is approximately three times as effective in $\overline{r^2}$ as the slowing material.
This concept is applicable for a small cavity and is evident from the approxima-
tion given by Serber for small a

$$\overline{r^2} \simeq \overline{r_0^2} + 3a^2 - 2\sqrt{6/\pi}\, a^3/r_0$$

For a large compared with r_0, he has given

$$\overline{r^2} \simeq a^2 + \left(4/\sqrt{6\pi}\right) ar_0$$

which may be noted is suggested by the simple physical concept for this case:

$$\overline{r^2} = (r_0 + a)^2 \qquad \text{for} \quad r_0 \ll a$$

The case for the data analyzed above is an intermediate one and therefore the exact expression has been used.

It is evident from these data that normal uranium has a large inelastic scattering for Ra-Be and Ra-B neutrons and that such scattering is accompanied by a large energy loss. The rather definite distinction between primary and scattered neutrons suggests the absence of intervening levels from which inelastically scattered neutrons might be emitted. It would be of considerable interest to extend the method to sources of different energies and to other materials.

A. C. Graves and J. C. Hoogterp have assisted in the evaluation of the data, and several discussions with R. Serber have been very helpful.
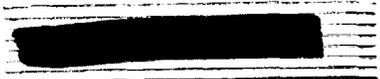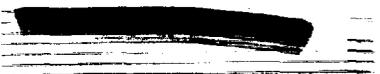
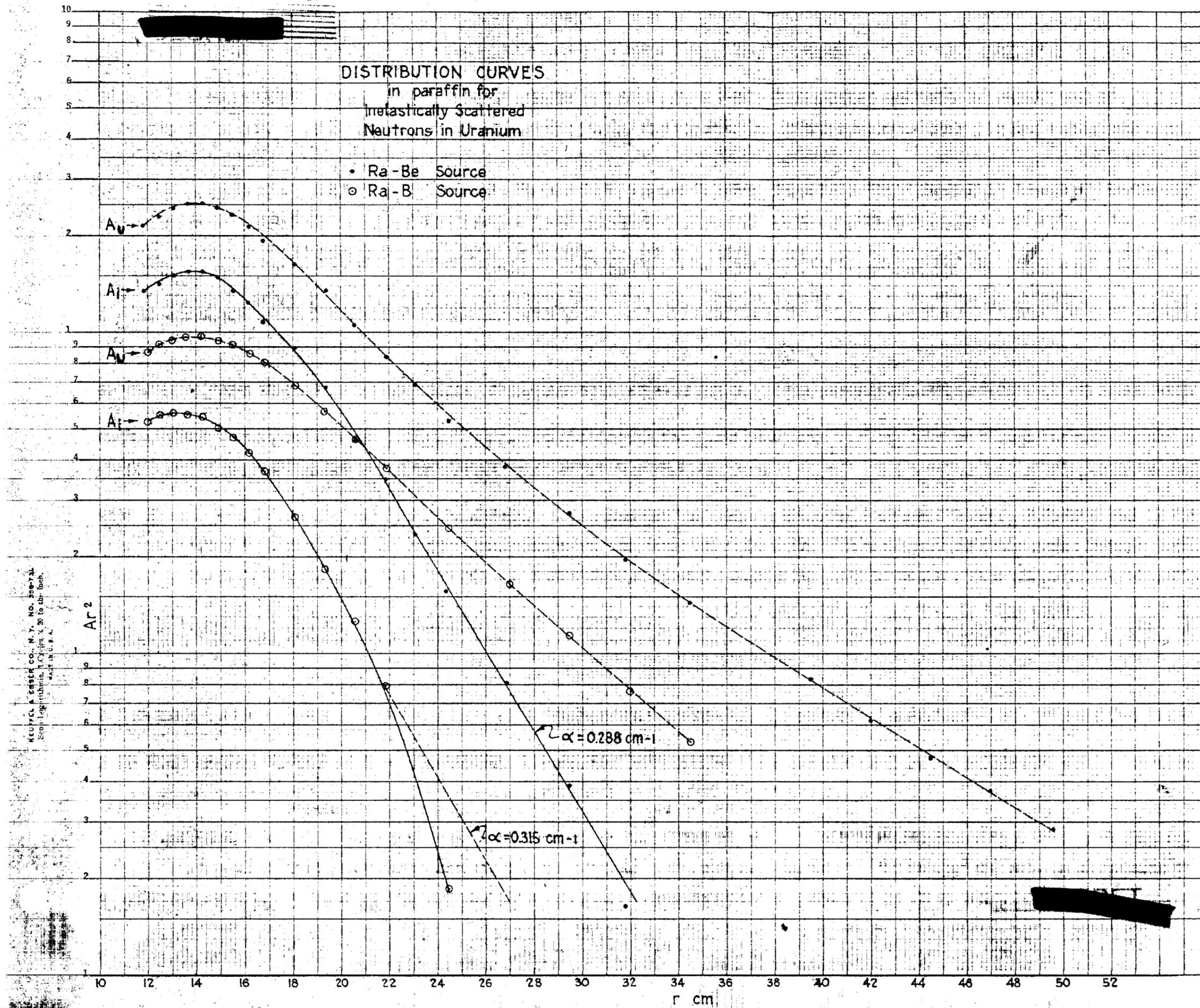## TABLE I

Ra-Bo Data -- $f = 0.60$
$\sigma_i = 2.5$
$E = 1.13$

	α	En Mev	r^2 cm²	r_o^2 cm²	r_o^2 cm² Water	En Mev
A_o	0.105	4.4	584	238	295	4.1
A_i	0.288	0.2	292	54.3	67.3	0.25

Ra-B ## TABLE II

Ra-B Data -- $f = 0.66$
$\sigma_i = 2.4$
$E = 1.053$

	α	En Mev	r^2 cm²	r_o^2 cm²	r_o^2 cm² Water	En Mev
A_o	0.1515	2.5	500	150	186	2.1
A_i	0.315	0.10	260	37.6	46.6	0.08

DISTRIBUTION CURVES
in paraffin for
Inelastically Scattered
Neutrons in Uranium

• Ra-Be Source
◦ Ra-B Source

$\alpha = 0.288$ cm-1

$\alpha = 0.315$ cm-1

Ar^2

r cm

Attention has been called to a numerical error which reduces the value of $\sigma' = 3.0$ b on page 7.

The difficulty of obtaining a reasonably precise value lies in the discrepancy in CF-1177 concerning the sphere. On the basis of the stated density of 18 and a path length of $5.5 - 1.0$ cm $= 4.5$ cm,

RaBe $\qquad \sigma' = 2.7$ b

RaB $\qquad \sigma' = 2.2$ b.

However, CF-1177 also gives the radius of 5.5 cm and mass 11,200 grams or a density of only slightly over 16. Hence

RaBe $\qquad \sigma' = 2.5$ b

RaB $\qquad \sigma' = 2.0$ b.

One must therefore state a range for the inelastic cross section;

RaBe $\qquad \sigma'_i = 2.0$ to 2.2 b

RaB $\qquad \sigma'_i = 1.5$ to 1.7 b.